Quantification of infectious agents transmission in pigs: Mathematical modelling of experimental and field data.

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Outline

Introduction

- Model building
- Model parameters
- Data and parameter inference
- Experimental facilities

2 Parameter Estimation

- PCV-2 Direct and Indirect Transmission
- PCV-2 Time-dependent Transmission
- Dealing with quantitative data

Oiscussion and Warnings

Model building Model parameters Data and parameter inference Experimental facilities

Model building

An infectious disease is often characterized by its

- transmission route
- transmission potential
- natural history
 - incubation time
 - Iatent period
 - infectious period
- acquired immunity
- symptomatic/asymptomatic

Identification of these characteristics is essential for realistic modelling assumptions.

Model building Model parameters Data and parameter inference Experimental facilities

Symboles and notations

Entity	Symbol 1	Symbol 2
Maternal immune	M (number)	m (proportion)
Susceptibles	S (number)	s (proportion)
Infected	I (number)	i (proportion)
Recovered	R (number)	r (proportion)
New cases	C (number)	c (proportion)
Total population size	N (number)	-
Recovery rate	γ (rate)	-
Force of infection	λ (rate)	-
Transmission parameter	β (rate)	-
Basic reproduction number	R_0 (dec. number)	-

Table: Commonly (and non-exhaustive) notations in epidemiological model

Model building Model parameters Data and parameter inference Experimental facilities

Model parameters

Once the conceptual model is built, questions remain:

- What are the underlying parameters, their meanings and/or interpretations?
- Is there any information on their values in literature?
- What kind of data could allow for parameter inference?
- How could we use these data whenever they were available?
- Are such data available in the literature?
- Is it possible to generate such data?

Model building Model parameters Data and parameter inference Experimental facilities

Data and parameter inference

Parameter estimation from available data is often challenging for multiple reasons:

- Data are often sparse.
- Transmission process is partially observed.
- Data are mostly based on case notifications (*i.e.* only symptomatic cases are reported).
- The exact time of infection is unknown.
- External factors can modify the course of infection.

In this context, experimental transmission trials offer the opportunity to study specific aspects of transmission in fully controled environment.

Model building Model parameters Data and parameter inference Experimental facilities

Experimental facilities

- All experiments were carried out in level 3 biosecurity air-filtered facilities.
- Specific Pathogen Free pigs were derived from Anses' confined pig herd.



Parameter estimation from experimental trials

Porcine CircoVirus of type 2

Context

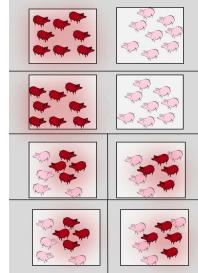
- Small DNA virus widely prevalent in pig herds
- Aetiologic agent of Postweaning Multisystemic Wasting Syndrome (PMWS)
- Vertical and horizontal transmission
- Huge protection confered by maternally derived antibodies

Objectives

- Evaluation of transmission according to contact structure between animals
- Estimation of the duration of the infectious period
- Estimation of the basic reproduction number (R_0) for PCV-2

Experimental settings

- 72 SPF pigs aged 4 weeks
 - 8 negative control
 - 32 inoculated pigs
 - 32 Sentinel pigs
- Inoculation with 6mL of suspension titrating $10^5 \ {\rm TCID}_{50}$
- Blood samples twice-a-week until 42 DPI
 - Virology: Real-time PCR
 - Serology: Elisa test



Modeling Hypotheses

- SEIR model $\implies R_0 = \beta/\gamma$
- Animals with positive PCR results are considered infectious.
- Latent period fixed to 6 days for contact pigs.
- Three assumptions for individual duration of infectious periods:
 - H1: Seroconversion
 - H2: Seroconversion + decline of virological titers
 - H3: Constant infectiousness throughout the trial

Parameter estimation

- Survival analysis for the duration of infectious period
- Transmission Rate: Maximum likelihood method
 - Individual probability to escape infection on time-interval $[t_j; t_{j+1}]$:

$$p_j = exp(-(\beta_w I_j^w/N_j^w + \beta_b I_j^b/N_j^b) \Delta_j)$$

• Number of new cases follows a binomial distribution

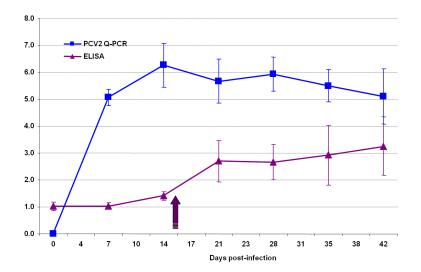
$$C_j \sim Bin(S_j, 1-p_j)$$

• Likelihood expression:

$$L = \prod_{g=1}^{nGroups} \prod_{j=1}^{nObs} dBin(S_j^g, 1 - p_j^g)$$

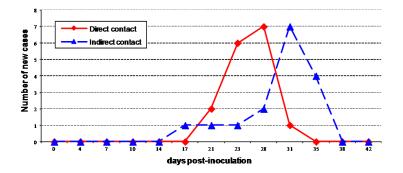
PCV-2 Direct and Indirect Transmission PCV-2 Time-dependent Transmission Dealing with quantitative data

Virological and Serological results



PCV-2 Direct and Indirect Transmission PCV-2 Time-dependent Transmission Dealing with quantitative data

Incidence in contact groups



- Surprisingly the first case was in indirect contact group.
- Peak of incidence was ealier in direct contact group.

Parameter Estimation Discussion and Warnings

PCV-2 Direct and Indirect Transmission

Quantification of transmission

Parameter	Hypothesis								
	H1	H2	H3						
β_w	0.26 [0.18-0.38]	0.22 [0.14-0.34]	0.19 [0.12-0.30]						
β_b	0.03 [0.01-0.06]	0.03 [0.02-0.08]	0.04 [0.02-0.08]						
γ	0.06 [0.04-0.08]	0.03 [0.02-0.04]	-						
$1/\gamma$	17.9 [12.5-25]	34.6 [23.9-50.2]	-						
R_{0w}	4.7 [2.9-7.6]	7.7 [4.3-13.5]	-						
R_{0b}	0.47 [0.19-1.17]	1.2 [0.5-2.9]	-						

Conclusions

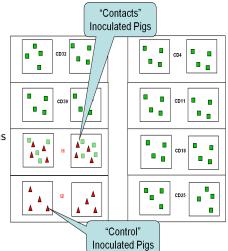
- R_{0b} relatively low but further cause of within-group transmission $\implies R_{0b}$ not negligible
- Huge impact of the assumption on the duration of infectious period on R_0 estimates.
- H2 biologically likely:
 - appearance of neutralizing antibodies
 - decrease of viral load.

Complementary experimental trial to study in depth:

- The **duration of the infectious period**, *i.e* the time during wich an infected animal effectively transmit the virus to susceptible host.
- the evolution of infectiousness according to time since infection.

Experimental design

- 72 SPF pigs aged 3 weeks
 - 8 negative control
 - 16 inoculated pigs
 - 48 Sentinel pigs
- Inoculation as in the previous study
- Weekly blood sampling
 - Virology: Real-time PCR
 - Serology: Elisa test



Parameter Estimation

Definition

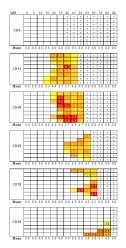
- τ : time since infection
- β(τ): average number of new cases produced by an individual infected since τ units of time.

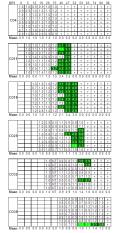
Consequences

- $\int_0^\infty \beta(\tau) d\tau$: average number of cases produced by an individual during its entire infectious period.
- Individual probability to escape infection on time-interval $[t_j; t_{j+1}]$: $p_j = exp(-I_j \int_{t_j}^{t_{j+1}} \beta(\tau) d\tau)$
- Likelihood expression: $L = \prod_{g=1}^{nGroups} \prod_{j=1}^{nObs} dBin(S_j^g, 1 - p_j^g)$

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Virological and serological results

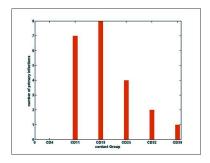




Primary cases: Due to contact with Inoculated pigs Secondary cases: Within-group transmission process Discrimination: 14 day-delay between first and next infections

Interpretation

Number of primary cases according to contact groups



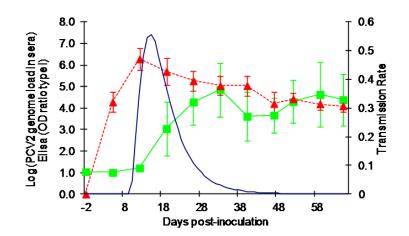
- Skewed distribution
- Mode: 11 18 DPI
- Left bounded (latency)
- Three functions tested:
 - Gamma-like,
 - Log-Normal-like,
 - Weibull-like,

defined as the product of R_0 with the related **probability** density function.

For each function three parameters were estimated: R_0 and two parameters defining the probability density function.

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Time-dependent transmission



Conclusions

- Evidence of time-varying transmission.
- Basic reproduction number for PCV-2 estimated to 5.9 (1.8;10.1).
- Transmission rate vanishes (< 0.001) 56 days post-infection.
- Qualitative relationship between transmission, viremia and serology.

Could we relate quantitative laboratory analysis to transmission?

Fluoroquinolone-Resitant E. coli

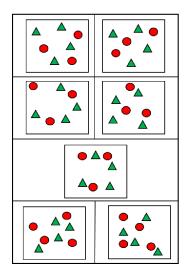
Context

- Antimicrobial resistance: public health issue.
- \bullet Persistence and spread of resistant bacteria \implies treatment failures
- \bullet Quinolones widely used in pig production \implies selective pressure. Objective

Quantifying the transmission of FQ-resistant E. coli in pig population

Fluoroquinolone-Resitant E. coli

- 65 SPF pigs (3 weeks post-weaning)
 - 6 negative control
 - 8 inoculated control
 - 23 inoculated (contact) pigs
 - 28 Sentinel pigs
- Inoculation: 10 mL suspension (10^9 CFU/mL)
- Fecal sampling:
 - daily from 0 to 4 DPI
 - every 2 days until 10 DPI
- Bacterial counts(BC).



Model hypotheses

- Susceptible-Infectious-Susceptible (SIS)
- Susceptible: $BC < 5 \ 10^3$ (CFU/g of feces)
- Infectious individual distributed according to three assumption
 - H1: All individuals have equal transmission potential (I_L)
 - H2: Two infectious states:

$$I_L \text{ if } 5 \cdot 10^3 < BC < 10^6$$

 $I_H \text{ if } BC > 10^6$

• H3: Three infectious states:

$$\begin{array}{l} I_L \text{ if } 5 \cdot 10^3 < BC < 10^5 \\ I_M \text{ if } 10^5 < BC < 10^6 \\ I_H \text{ if } BC > 10^6 \end{array} \end{array}$$

Parameter estimation

- Survival analysis for the duration of infectious period
- Transmission Rate: Maximum likelihood method
 - Individual probability to escape infection on time-interval $[t_j; t_{j+1}]$:

$$p_j = exp(-(\beta_L I_{Lj}/N + \beta_M I_{Mj}/N + \beta_H I_{Hj}/N) \Delta_j)$$

• Number of new cases follows a binomial distribution

$$C_j \sim Bin(S_j, 1-p_j)$$

Likelihood expression:

$$L = \prod_{g=1}^{nGroups} \prod_{j=1}^{nObs} dBin(S_j^g, 1 - p_j^g)$$

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Results

Hypothesis	Parameters								
	β_L	β_M	β_H						
H1	0.55 (0.40; 0.74)	-	-	121.00					
H2	0.41 (0.27; 0.62)	-	0.98 (0.59; 1.62)	117.85					
H3	0.41 (0.23; 0.71)	0.42 (0.15;1.19)	0.98 (0.59; 1.62)	119.85					

Conclusions

- Transmission dependent on the quantity of bacteria shed in feces
- No appearent role of the intermediate level:
 - Transient state
 - low number of animal simultaneously in this compartment
- the basic reproduction number was not estimated:
 - the dose-dependent transmission
 - the variability in individual shedding
 - the evidence of host reinfection
- Only **horizontal transmission** was considered when **oro-fecal** transmission is more likely.

In this particular case, **environmental reservoir** should play a non-negligible role in transmission.

Hepatitis E virus transmission

Context

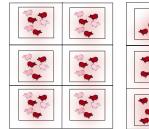
- Hepatitis E is a zoonotic disease.
- Clinical expression similar to hepatitis A in humans.
- Possible chronic infections in immunocompromised humans.
- Pigs are considered as the main reservoir.
- Totally asymptomatic in pigs.
- Oro-fecal transmission is predominant.

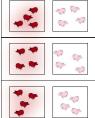
Objective

- Estimating HEV transmission in pigs.
- Disentangling the different transmission routes: horizontal (direct contacts) and environmental transmission.

Experimental design

- 68 SPF pigs (5 weeks)
 - 8 negative control
 - 30 inoculated (contact) pigs
 - 30 Sentinel pigs
- Oral inoculation: 10 mL suspension (10^8 ge/mL)
- Fecal sampling: 3-times a week for 39 days.
- Virology: Quantitative RT-PCR.
- Serology: Elisa test.





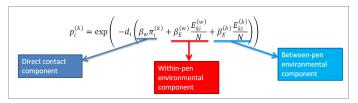
Modeling framework

Environmental Component

- Average quantity of virus shed within a specific pen
- Accounting for a daily clearance rate (δ)

$$E_{ki} = E_k(t_{i+1}) = (E_k(t_i) + \int_0^{\Delta_t} V_k(t_i + u)e^{\delta u} du)e^{-\delta \Delta t}$$

Probability to escape from infection



Likelihood expression

- Assumption: A pig is infectious when fecal samples are positive for HEV.
- Date of infection: Any time prior to the first positive sample.
- This time has to be wheighted by the duration of latency period.

Individual contribution to Likelihood

$$L^{(j)}\left(\mathbf{D}_{\mathbf{I}}, \pi_{\mathbf{w}}, \mathbf{E}, \beta_{w}, \beta_{E}^{(w)}, \beta_{E}^{(b)}, A, B, \delta\right) = \sum_{i=1}^{I_{j}} \left\{ \prod_{l=1}^{i} p_{l-1}^{(k)} (1-p_{i}^{(k)}) f_{Lat}(t_{I_{j}}-t_{i}, A, B) \right\}$$

Likelihood

$$L\left(\mathbf{D}_{\mathbf{I}}, \pi_{\mathbf{w}}, \mathbf{E}, \beta_{w}, \beta_{E}^{(w)}, \beta_{E}^{(b)}, A, B, \delta\right) = \prod_{j=1}^{nC} L^{(j)}\left(\mathbf{D}_{\mathbf{I}}, \pi_{\mathbf{w}}, \mathbf{E}, \beta_{w}, \beta_{E}^{(w)}, \beta_{E}^{(b)}, A, B, \delta\right)$$

Bayesian inference using Metropolis-Hasting Algorithm.

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Results

Virology direct contact groups

										m'g of foces								
	DPI	1	3	6	8	10	13	15	17	20	22	24	28	31	34	36	38	44
Room1. Group 1	Inoculated	0	0	0	0	0	3.58 10	2.0710	8.7210	1.27 104	0	0	0	0	0	0	0	-
	Inoculated	0	0	4.39 104	7.89104	5.54 105	2.75 105	5.40 104	2.45 104	2.14 104	0	0	0	0	0	0	0	0
	Inoculated	0	0	0	0	0	2.39 104	3.37 104	2.98 104	1.70104	1.10 104	0	0	0	0	0	0	4
	Contact	0	0	0	0	0	0	0	0	0	3.09104	1.20 10	5.12 10 ⁴	6.55104	0	0	0	0
	Contact	0	0	0	0	0	0	0	0	0	0	8.82 10 ³	4.47.104	3.66104	7.80103	0	0	4
	Contact	0	0	0	0	0	0	0	0	0	1.08 104	1.25 104	3.56 104	0	0	0	0	-
Room1. Group 2	Inoculated	0	0	0	0	1.33 104	9.52 10	1.2710	8.37104	7.41103	0	0	0	0	0	0	0	
	Inoculated	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	- 0
	Inoculated	0	0	0	0	9.78 104	2.99 10 ⁵	9.9010	2.55104	0	0	0	0	0	0	0	0	
	Contact	0	0	0	0	0	0	0	0	0	0	1.06 104	0	0	0	0	0	- 4
	Contact	0	0	0	0	0	0	0	0	0	1.53 104	1.30 10*	0	0	0	0	0	0
	Contact	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	4
com2. Group 3	Inoculated	0	0	0	0	3.03104	0	0	0	0	0	0	0	0	0	0	0	
	Inoculated	0	6.63 10 ³	3.88104	2.28 10	9.77 104	2.74 108	1.43 10 ⁶	2.69 104	0	0	0	0	0	0	0	0	- 6
	Inoculated	0	0	2.23 104	0	3.65104	4.17 104	2.58 10 ⁶	0	0	0	0	0	0	0	0	0	- 9
	Contact	0	0	0	0	0	0	9.03 104	1.99 10	3.0310	2.86 10 ⁵	0	0	0	0	0	0	- 0
	Contact	0	0	0	0	0	0	2.16 104	2.73 105	0	0	0	0	0	0	0	0	
	Contact	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	
loom2. Group 4	Inoculated	0	0	0	0	0	0						0	0	0	0	0	4
	Inoculated	0	0	0	6.05104	5.51 104	2.58 10		14	days	s		0	0	0	0	0	0
	Inoculated	0	0	0	1.79104	1.21104	1.83 10	```				\rightarrow	0	0	0	0	0	4
	Contact	0	0	0	0	0	0						0	0	0	0	0	0
	Contact	0	0	0	0	0	0						1.15104	0	0	0	0	- 9
	Contact	0	0	0	0	0	0		0	0	0	0	0	9.05104	3.38104	0	0	-
loom3. Group 5	Inoculated	0	0	0	0	1.97 104	2.24 105	3.68 10	4.06 104	0	0	0	0	0	0	0	0	-
	Inoculated	0	0	0	5.27104	3.34 104	1.24 10 ⁵	2.59 105	5.03 105	1.57 103	0	0	0	0	0	0	0	
	Inoculated	0	0	0	7.16104	1.20 10 ⁵	7.47 10 ⁵	1.0610	4.51 10 ⁵	1.57105	2.72 104	8.24 10	0	0	0	0	0	
	Contact	0	0	0	0	0	0	0	0	0	0	0	0	1.78104	0	2.88 10*	0	
	Contact	0	0	0	0	0	0	0	0	0	0	0	1.75 104	2.65104	0	0	0	
	Contact	0	0	0	0	0	0	0	0	0	0	0	9.60 10 ³	0	1.07 104	5.39 10 ⁴	0	0
com3. Group 6	Inoculated	0	0	0	0	0	7.20 10	2.23 10	4.01 104	7.12104	1.6610	2.67 104	0	0	0	0	0	
	Inoculated	0	0	0	0	2.36103	7.73 104	9.68 104	3.06 10 ⁵	0	0	0	0	0	0	0	0	
	Inoculated	0	0	0	8.82103	1.34 10 ⁵	3.71 10 ⁵	2.38 10 ⁶	1.94 10 ⁶	2.41104	0	0	0	0	0	0	0	- 4
	Contact	0	0	0	0	0	0	0	0	0	1.03 104	1.47 10	6.08 10	1.3810	1.17 10	7.76 10	0	- 9
	Contact	0	0	0	0	0	0	0	0	0	1.12 10 ⁵	4.58 10 ⁴	1.15105	2.14 105	4.65105	0	0	
	Contact	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	

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Results

Virology indirect contact groups

									HE	/ geig of fece	5							
	DPI	1	3	0	8	10	13	15	17	20	22	24	28	31	34	38	38	
Room 4, Group a	Inoculated	0	0	3.34104	0	2.63 104	2.85 104	0	0	0	0	0	0	0	0	0	0	
	Inoculated	0	0	1.77104	2.57 104	1.58104	1.01 10	4.5210	0	0	0	0	0	0	0	0	0	
	Inoculated	0	4.90 103	4.72104	8.69104	2.0910	9.2510	1.75 10	2.13.104	5.46104	0	0	0	0	0	0	0	
	Inoculated	0	3.80 10 ³	1.1510	2.1810	1.37 10	5.98 10	2.3910	0.4410	1.7010	1.23 10	4,81104	0	0	0	0	0	
Room 4, Group b	Contact	0	0	0	0	0	0	0	0	0	0	0	0	1.18104	2.75104	0	0	
	Contact	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	8.77
	Contact	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1.90
	Contact	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0		9.50
													-				-	
Room 6, Group a	Inoculated	0	1.30 104	1.30 104	1.30 104	1.30104	1.30104	1.30 104	1.30 104	1.30104	0	0	0	0	0	0	0	
	Inoculated	0	0	0	0	7.00104	6.34 10	3.5510	3.27 104	0	0	0	0	0	0	0	0	
	Inoculated	0	0	7.25104	2.40104	2.47 10	1.0810	4.87 10	1.47 104	1.10104	0	3.48104	0	0	0	0	0	
	Inoculated	0	0	8.41104	2.70 10	0.0310	4.0910	4.10 10	1.0510	1.40104	0	0	0	0	0	0	0	
loom 5, Group b	Contact	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	
	Contact	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	
	Contact	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	
	Contact	0	0	0	0	0	0	0	0	0	0	٥	0	0	0	0	0	
oom 8, Group a	Inoculated	0	0	0		1,1410	5.64 10	2.5410	7.22 10	7.33104	1.40 10	9.98104	5.19104	4.39104	0	0	0	
	inoculated	0	0	0		1.3710	1.09104	4.40104	0	0	0	0	0	0	0	0	0	
	Inoculated	0	0	0	0	7.70 10+02	9.0810	1.64 10	0	0	0	0	0	0	0	0	0	
	Inoculated	0	0	1.1010	1.61 10	4.8510	20410	474104	0	0	0	0	0	0	0	0	0	
bom 6, Group b	Contact	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	_
	Contact	0	0	0	0	0	0	0	0	0	0		0	0	0	0		
	Contact	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	
	Contact		0	0				0	0	0				0	0			

Introduction Parameter Estimation Discussion and Warnings Dealing with quantitative data

Results

Parameter		Estimates
	Median	95% CI
eta_w	0.15	(0.03; 0.31)
$\beta_E^{(w)}$	$2 \cdot 10^{-6}$	$(1 \cdot 10^{-7}; 7 \cdot 10^{-6})$
$\beta_E^{(b)}$	$7\cdot 10^{-8}$	$(5 \cdot 10^{-9}; 3 \cdot 10^{-7})$
A	5.3	(3.2; 8.7)
В	0.76	(0.48; 1.25)
δ	0.33	(0.19; 0.46)

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Conclusions

Remark

 $\beta_E^{(w)}: \mbox{Average number of new cases produced by a one ge/g of feces in the environment.}$

 $\Rightarrow \varepsilon = \beta_E^{(w)-1}$ corresponds the the average quantity of virus per gram of feces necessary to infect one individual.

 $\varepsilon = 5.62 \cdot 10^5 \text{ge/g} (1.45 \cdot 10^5; 9.34 \cdot 10^6).$

- Direct contacts:
 - Sufficient to explain the maintenance of virus in infected pig herds
 - not enough to explain the high prevalences recorded in field conditions
- First clear evidence of environmental transmission:
 - Sustained increase of the force of infection
- indirect transmission via the environment
 - Rare events
 - Not negligible since inducing further within-pen transmission.

Analysis of experimental transmission trials...

... presents several advantages:

- Controlled environment
- Investigations on specific aspects
 - Contact structure
 - Vaccination
 - Passive immunity
 - Role of environmental factors

But...

Analysis of experimental transmission trials...

... have to be considered with care because far from field conditions

- Pigs are SPF
- Environment is fully controlled
- No external risk factors (co-infections)

Analysis of experimental transmission trials...

Moreover practical issues have to be considered

- Ethics
- Biosafety
- Heavy and expensive experimental designs
- Specific mathematical model and estimation methods
- Long process to be thought in advance

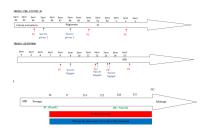


Figure: Time-scale for a SIV experiment with maternally derived immunity

Aknowledgements

- Pig Epidemiology and Welfare Unit
- Pig SPF Production and Experimental Unit
- Viral Genetics and Biosafety Unit
- Mycoplasmology-Bacteriology Unit
- Pig Immunology and Virology Unit
- UMR 1161 Virology/ ANSES/ ENVA/ INRA/ UPMC

Aknowledgements

Thanks for your attention

